# Marking Scheme – IGO2017 Advanced level

#### Problem 1:

Calculating  $\angle XIY$ : 2 points Calculating  $\angle IZB$ : 2 points Congruence of triangles *BIZ*, *BIA* and conclusion: 4 points

## Problem 2:

Complete proof (official solution): 8 points

Proving that it is sufficient to prove the statement for six unit circles: 3 points

Proving only the case of six unit circles: 5 points

## Problem 3:

Similarity of triangles *XOM*, *XPA*: 4 points

Conclusion: 4 points

# Problem 4:

*ZT* is the radical axis of  $\omega_1, \omega_3$ : 2 points

The midpoint of AC lies on the radical axis of  $\omega_1, \omega_3$ : 1 point

*ZB* equals to the length of tangent from *Z* to  $\omega_1$ ,  $\omega_3$ : 2 points

Calculating AC and conclusion: 3 points

## Problem 5:

Definition of  $P_{ab}$ s and  $W_a$ s: 2 points Inversion with center *P*: 2 points Considering Michel's point: 2 points Conclusion: 2 points

#### Marking Scheme – IGO2017

## **Elementary level**

#### Problem 1:

X = number of correct answers Y = number of incorrect answers If X = 0: 0 point If X > 0:  $Z = Max\{0, X - Y + 1\}$  points

## Problem 2:

Considering the rhombus and concluding the parallel lines: 2 points Calculating the angles (even in the figure): 3 points Calculating the angles of *ABC*: 3 points

## Problem 3:

AP = AF: 3 points CE = EF: 2 points BE = CE: 1 point Conclusion: 2 points

#### Problem 4:

Initial case: 1 point

The number of clockwise triangles changes one by one when the points move: 4 points

Final case: 1 point

Conclusion (there exists a moment with 2017 clockwise triangles): 2 points

# Problem 5:

Solution 1:

Considering the midpoints of *AB*, *AC* and their images in *l*: 2 points

Mentioning the inequalities for ME, NF: 2 points

Final calculation and conclusion: 4 points

Solution 2:

Considering the reflections of *P*, *E* (perhaps *D*), and presenting AP + AQ as length of a segment (*P'Q* in the solution): 3 points

 $P'Q \leq E'F$ : 2 points

 $E'F \leq AC$ : 3 points

# Marking Scheme – IGO2017

#### Intermediate level

#### Problem 1:

The side opposite to the 30-angle in a right triangle is half the length of the hypotenuse: 1 point

Calculating *CE*: 1 point Calculating *BF*: 1 point Final calculation and conclusion: 5 points

## Problem 2:

 $\angle BFD = \angle CEP$ : 2 points  $\angle BEP = \angle BFQ$ : 2 points Conclusion: 4 points

# Problem 3:

Complete example for n > 4: 3 points

(Correct example without mentioning the details worth 2 points)

n = 4 and convex quadrilateral: 3 points

n = 4 and concave quadrilateral: 2 points

The case n = 3 worth no point but if he/she forgot this case: -1 point

# Problem 4:

Solution 1:

Considering the midpoints of *AB*, *AC* and their images in *l*: 2 points Mentioning the inequalities for *ME*, *NF*: 2 points Final calculation and conclusion: 4 points Solution 2:

Considering the reflections of *P*, *E* (perhaps *D*), and presenting AP + AQ as length of a segment (*P'Q* in the solution): 3 points

 $P'Q \le E'F$ : 2 points  $E'F \le AC$ : 3 points

# Problem 5:

Mentioning equivalent statement (AMOA'N cyclic): 1 point Similarity of triangles A'KX, XM'X: 2 points Similarity of triangles A'KY, YN'N: 2 points Similarity of triangles A'NY, A'MX and conclusion: 3 points